



# JUNYUAN PRIMARY SCHOOL

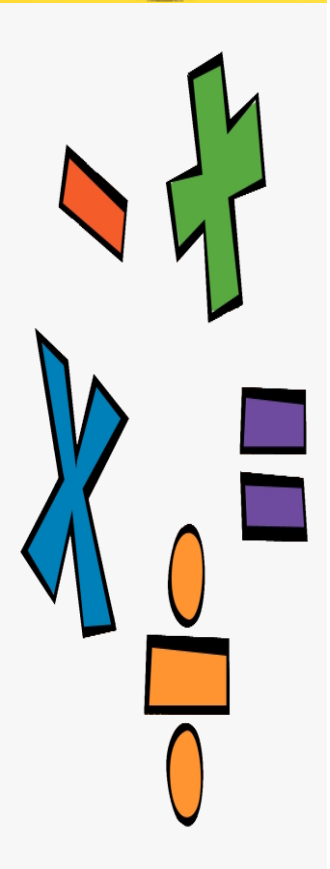
Welcome to

Primary 3 & Primary 4

Math Alive! 2024

Workshop for Parents

19 APRIL





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is under the property of  
**JUNYUAN PRIMARY SCHOOL**  
**Mathematics Department.**

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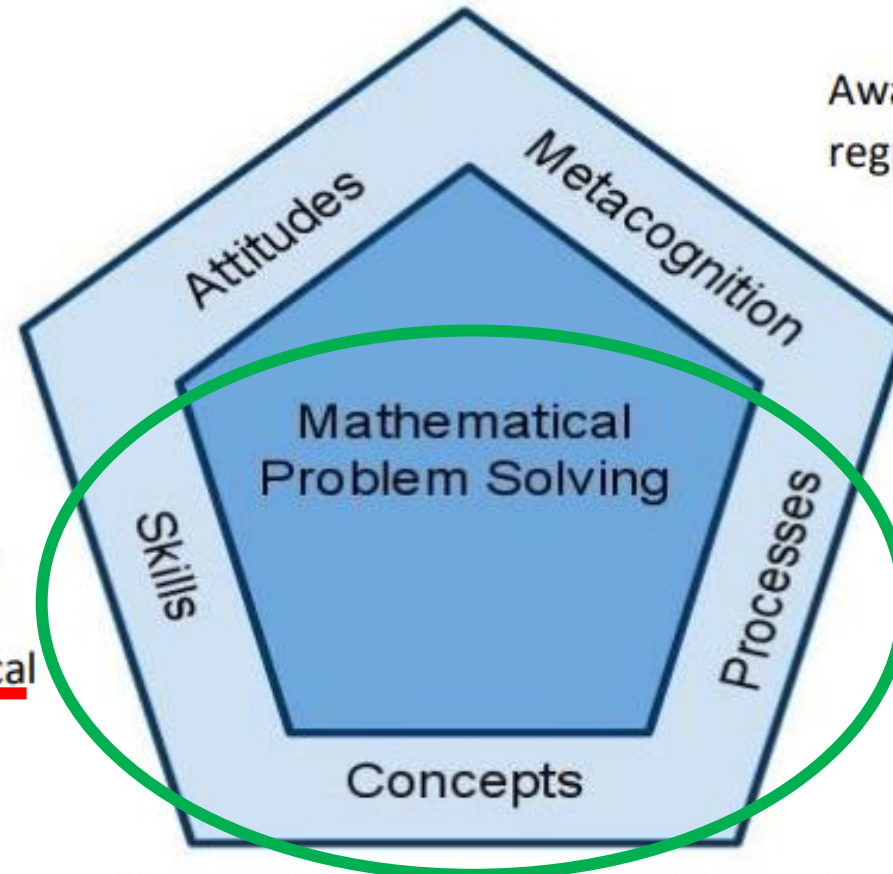
Thank you for your understanding and cooperation.

# Singapore Mathematics Framework

## Mathematics Curriculum Framework

Belief, appreciation,  
confidence, motivation,  
interest and perseverance

Awareness, monitoring and  
regulation of thought processes



Proficiency in carrying out  
operations and algorithms,  
visualising space, handling  
data and using mathematical  
tools

Competencies in abstracting  
and reasoning, representing  
and communicating,  
applying and modelling

Understanding of the properties and  
relationships, operations and  
algorithms

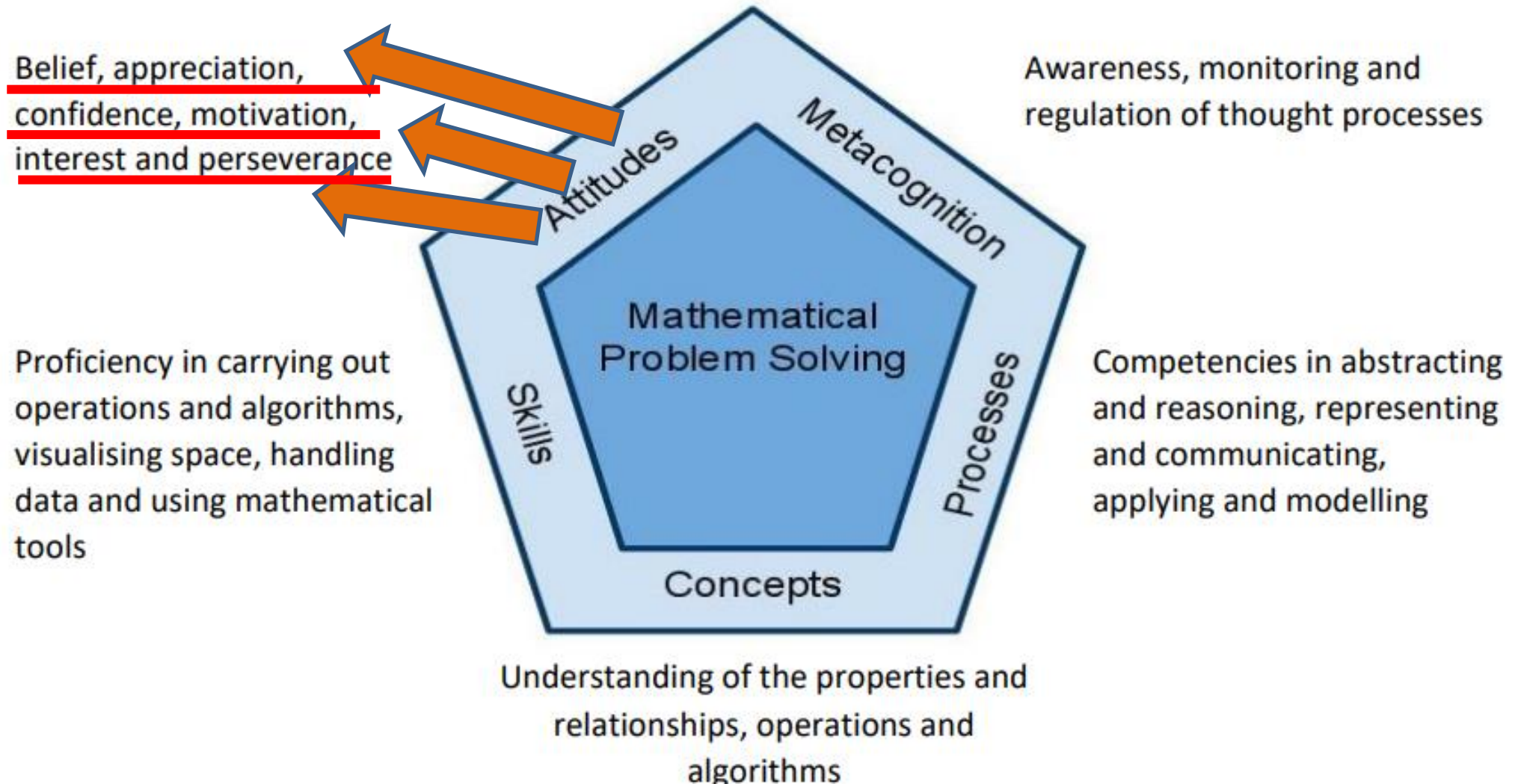
Conversion  
of units  
Perimeter  
Geometry  
Money  
Fractions  
Percentage

Bar Graph  
Area  
Volume  
Mass  
Decimals  
Algebra



# Singapore Mathematics Framework

## Mathematics Curriculum Framework



# Math Alive! In REAL LIFE DAILY APPLICATIONS





1 km = 1000 m

# Math Alive!



Junyuan Primary School, 2 Tampines Stre

Tampines Mall, 4 Tampines Central 5, Sin



via Tampines Ave 5

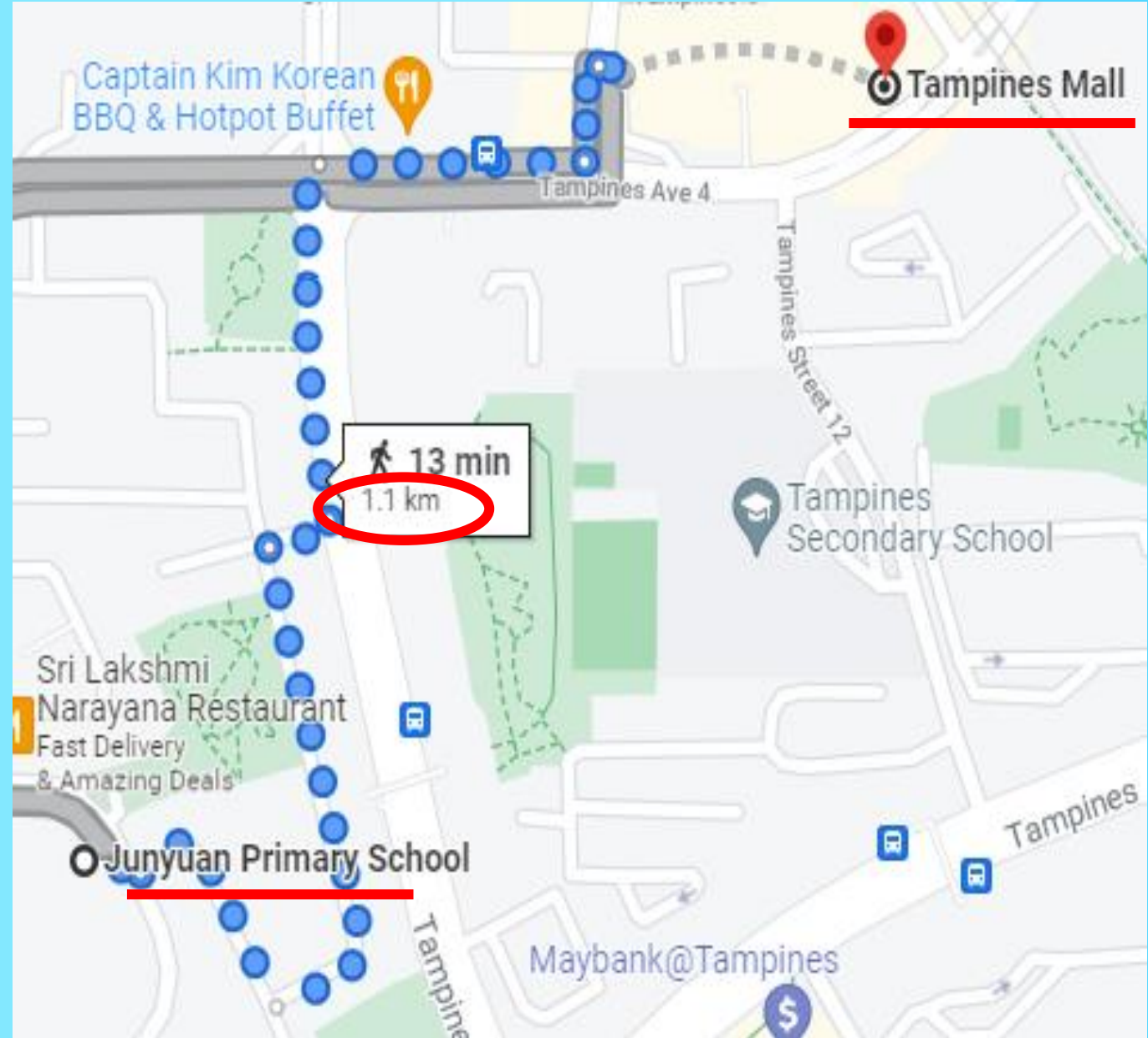
13 min

Mostly flat

1.1 km

**The distance from  
JYPS to Tampines Mall  
is about 1 km.  
Time taken is 13 min.**

Property Of Junyuan Primary School2024





# Math Alive!



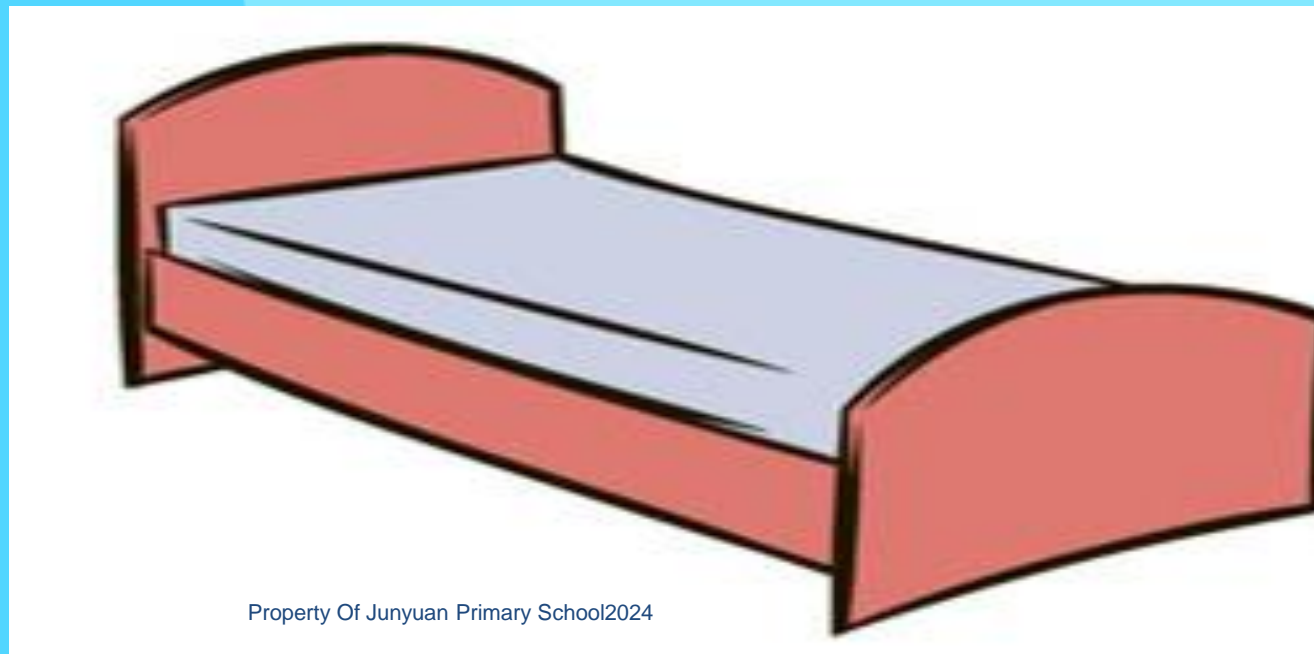
INGREDIENT	6-INCH
All-Purpose Flour	350 grams
Baking Powder	10 grams
Salt	3 grams
Butter, unsalted	254 grams
Granulated White Sugar	298 grams
Vanilla extract	5 grams
Eggs, large	4 pieces
Milk (Whole/ Full Fat)	273 grams
BAKING TIME ESTIMATE	40 minutes

1 cup butter or margarine  
1 ½ cups sugar  
4 eggs  
1 teaspoon vanilla extract  
½ teaspoon salt  
4 cups sifted cake flour  
4 teaspoons baking powder  
1 ⅓ cups milk





# Math Alive!



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# Math Alive!



## Thinking Aloud

Look at the cruise packages. Which is a better deal?



### 10 NIGHTS PACKAGE

- Cruise to Japan with a shopping stop-over in Hong Kong
- Mini-suites with personal attached balconies
- Indoor and outdoor movie theatre
- Wide spread of international cuisines available
- All day entertainment
- Free cooking and dance classes
- Free unlimited Wi-Fi

**\$3080**  
per person

Property Of Junyuan Primary School2024

## CRUISE *Tour*

### 7 NIGHTS PACKAGE

- Cruise to Australia and New Zealand
- Cruise cabins with ocean view
- Best cuisines for food lovers
- Endless engaging entertainment
- 24 hour gym facility
- Free unlimited Wi-Fi

**\$3080**  
per person



# Math Alive!



## Thinking Aloud



Mark needs 15 mini rolls for a party.

Which bakery should he buy from?

How many packets does Mark need to buy?



# Workshop Content

# 1) Introduction to Metacognition in Problem Solving using STAR approach

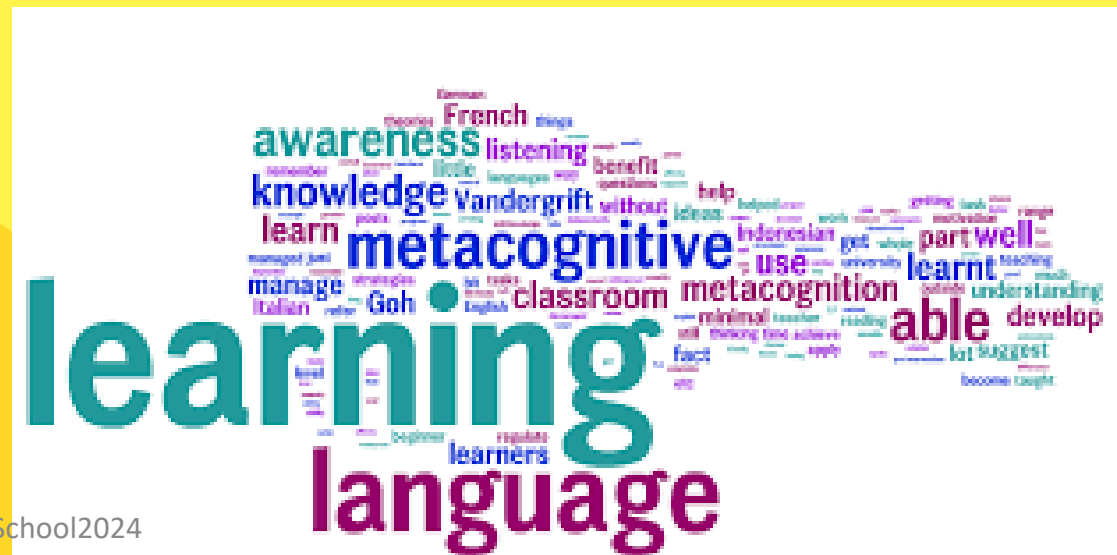
## 2) Heuristics of Problem Solving

### 3) KooBits

## 4) Q & A



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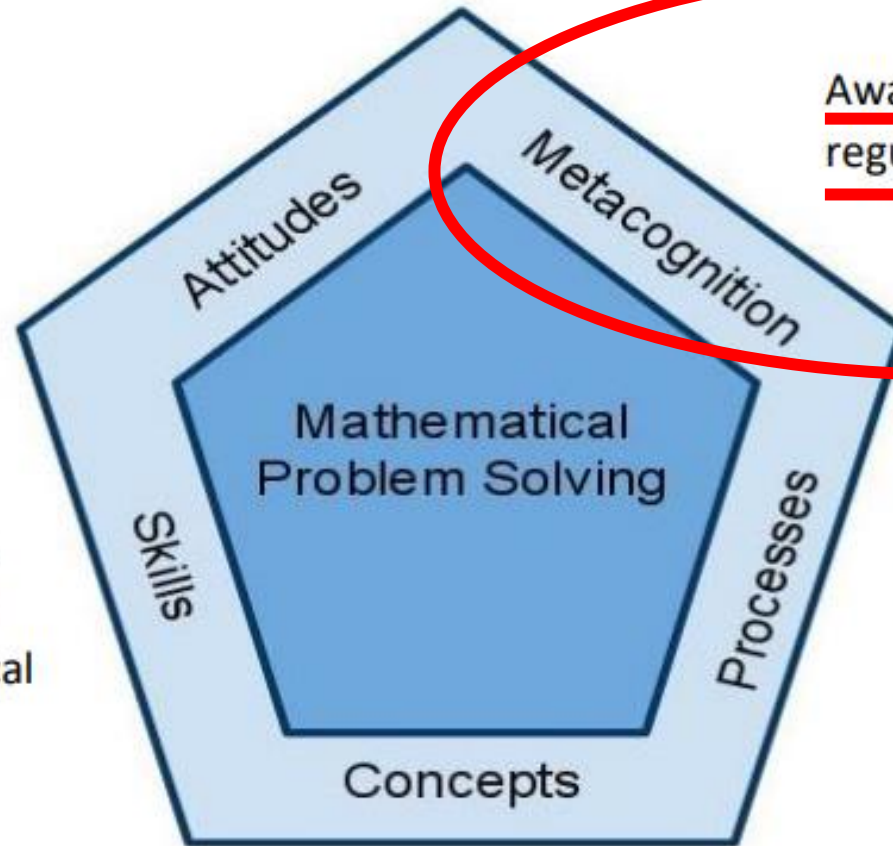


# Singapore Mathematics Framework

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Belief, appreciation,  
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Proficiency in carrying out  
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tools



Awareness, monitoring and  
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and reasoning, representing  
and communicating,  
applying and modelling

Understanding of the properties and  
relationships, operations and  
algorithms



# Metacognition

## Definition

Think about one's **own** thinking  
– To be critically **aware** of one's thinking and learning.

## Process

- **Monitor** one's own thinking and one's existing state of knowledge
- **Self-regulate** one's learning through goal setting, self-monitoring and self instruction

\* I'm thinking...  
\* I'm noticing...  
\* I'm wondering...  
\* I'm seeing...  
\* I'm feeling...  
\* I'm realizing...



# How to develop metacognitive awareness



- Exposure to general problem solving skills
- Thinking aloud using the strategies and methods taught
- Attempting problems that require planning and evaluation
- Seeking alternative ways to solve a problem
- Checking reasonableness of answers



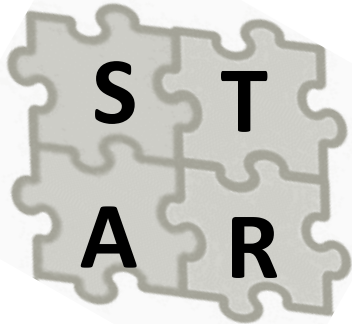
# Metacognition @ JYPS

JUNYUAN PRIMARY SCHOOL  
MATHEMATICS

# STAR

SEE ~ THINK ~ ACT ~ RELOOK

P4



NAME : \_\_\_\_\_

CLASS : P4 - \_\_\_\_\_

**S** - See (What is given?)

**T** - Think (What is my plan?)

Can I use Model Drawing?

Can I look for a pattern?

Can I work backwards?

Can I use Guess and Check?

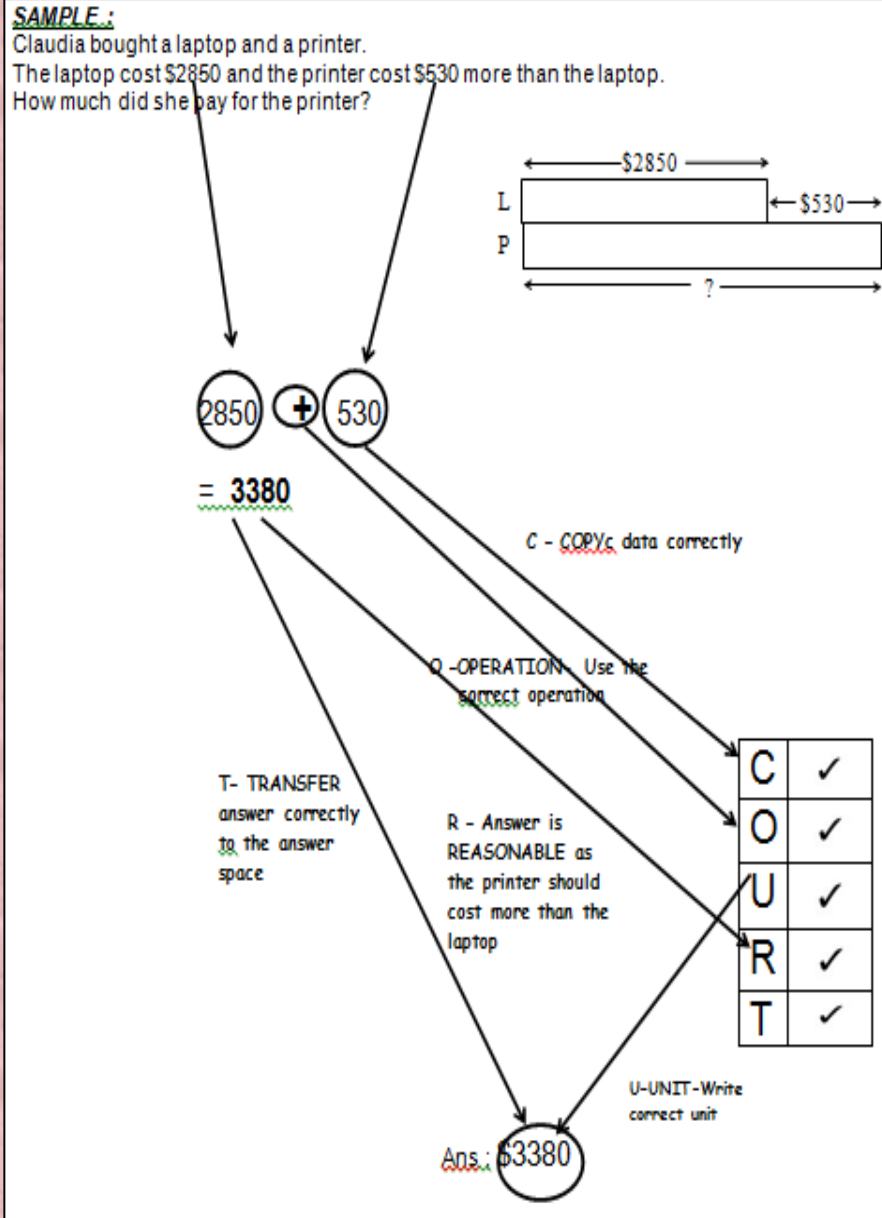
Other heuristic(s) I can use: \_\_\_\_\_

**A** - Act(What do I need to do?)

**R** - Relook(Reflect and Check)

# CHECKING Strategy Using

## C - O - U - R - T



**C** – Copy data correctly

**O** – Operation sign

**U** – Unit of measurement

**R** – Reasonableness of answer

**T** – Transfer answer correctly

C	
O	
U	
R	
T	



# Heuristics Of Problem Solving Model Drawing

- 1. Part-Whole Model***
- 2. Comparison Model***
- 3. Unitary Method**
- 4. Stacking Model**
- 5. Fraction of a Set**
- 6. Before and After**

# Q1: Model Drawing (Part-Whole) – Find Total

Aaron has 452 cards. Benedict has 373 cards.  
How many cards do they have altogether?

See (What is given?)

Aaron → 452

Benedict → 373

Altogether?

Think (What is my plan?)

✓ Can I use Model Drawing?

Can I look for a pattern?

Can I work backwards?

Can I use Guess and Check?

Other heuristic(s) I can use:

---

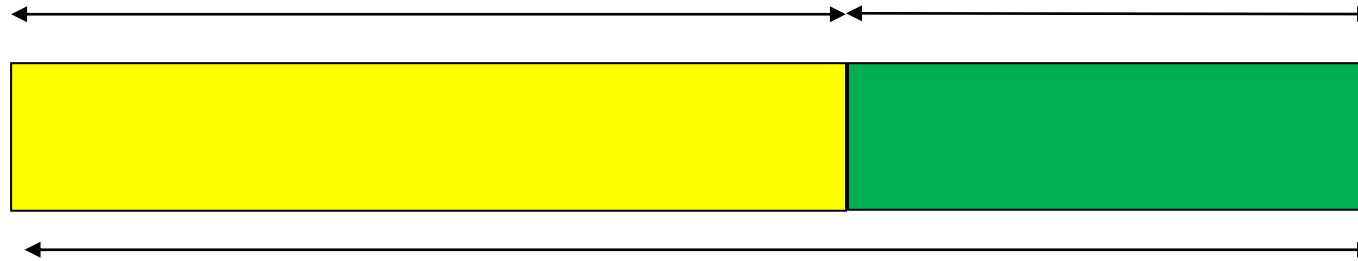


# Q1: Model Drawing (Part-Whole) – Find Total

Act (What do I need to do?)

452

373



? (+ )

Method

$$452 + 373 = 825$$

They have **825 cards** altogether.

# Q1: Model Drawing (Part-Whole) – Find Total

Aaron has 452 cards. Benedict has 373 cards.  
How many cards do they have altogether?

Act

Method

$$452 + 373 = 825$$

Relook (Reflect and Check)

$$\$825 - 373 = \$452 \quad \checkmark \text{ok}$$

C	<input checked="" type="checkbox"/>
O	<input checked="" type="checkbox"/>
U	<input checked="" type="checkbox"/>
R	<input checked="" type="checkbox"/>
T	<input checked="" type="checkbox"/>



## Q2: Model Drawing (Part-Whole) – Find Part

Rachel and Sally have 263 hair clips altogether.

Sally has 91 hair clips.

How many hair clips does Rachel have?

**See (What is given?)**

Rachel & Sally → 263

Sally → 91

Rachel ?

**Think (What is my plan?)**

✓ Can I use Model Drawing?

Can I look for a pattern?

Can I work backwards?

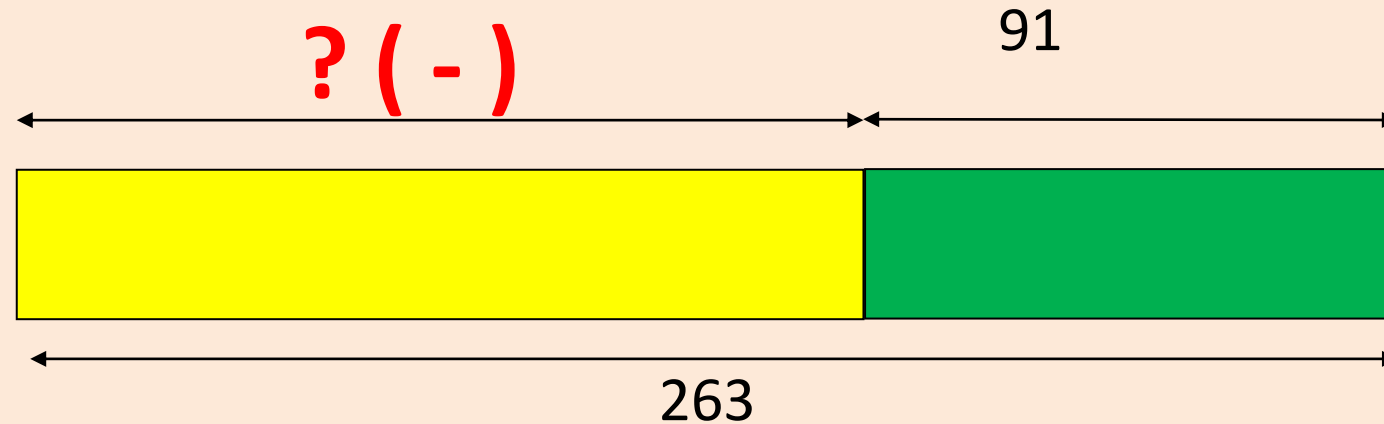
Can I use Guess and Check?

Other heuristic(s) I can use:

---

## Q2: Model Drawing (Part-Whole) – Find Part

Act (What do I need to do?)



Method

$$263 - 91 = 172$$

Rachel has **172** paper clips.



## Q2: Model Drawing (Part-Whole) – Find Part

Rachel and Sally have 263 hair clips altogether.

Sally has 91 hair clips.

How many hair clips does Rachel have?

Act

Method

$$263 - 91 = 172$$

Relook (Reflect and Check)

$$172 + 91 = 263 \quad \checkmark \text{ ok}$$

C	✓
O	✓
U	✓
R	✓
T	✓

# Q3: Model Drawing

## (Comparison with 2 variables) – Finding Difference

Hotel Pan Pacific Singapore charges \$330 per night. Hotel Amara Singapore charges \$198 per night. How much will Mr Ong save if he decides to stay in Amara Singapore instead of Pan Pacific Singapore for three nights?

See (What is given?)

Pan Pacific → \$330

Amara → \$198

Save?

Think (What is my plan?)

✓ Can I use Model Drawing?

Can I look for a pattern?

Can I work backwards?

Can I use Guess and Check?

Other heuristic(s) I can use:

---

# Q3: Model Drawing

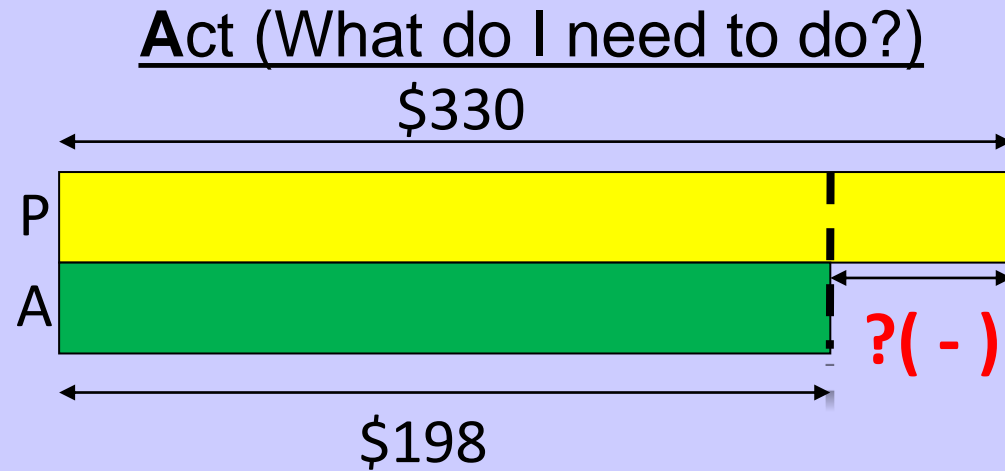
## (Comparison with 2 variables) – Finding Difference

See (What is given?)

Pan Pacific → \$330

Amara → \$198

Save?



Method

$$\$330 - \$198 = \$132$$

$$\$132 \times 3 = \mathbf{\$396}$$

Mr Ong will save **\$396**.



# Q3: Model Drawing

## (Comparison with 2 variables) – Finding Difference

Hotel Pan Pacific Singapore charges \$330 per night. Hotel Amara Singapore charges \$198 per night. How much will Mr Ong save if he decides to stay in Amara Singapore instead of Pan Pacific Singapore for three nights?

Method

$$\$330 - \$198 = \$132$$

$$\$132 \times 3 = \underline{\underline{\$396}}$$

Relook (Reflect and Check)

$$\$396 \div 3 = \$132$$

$$\$132 + \$198 = \$330 \quad \checkmark \text{ ok}$$

Mr Ong will save \$396.

C	<input checked="" type="checkbox"/>
O	<input checked="" type="checkbox"/>
U	<input checked="" type="checkbox"/>
R	<input checked="" type="checkbox"/>
T	<input checked="" type="checkbox"/>

# Q4: Model Drawing

## (Comparison with 2 variables – Unequal Distribution)

At a factory, Worker A and Worker B sorted 1886 plastic bottles altogether. Worker B sorted 988 more bottles than Worker A. How many bottles did Worker A sort?

See (What is given?)

$A + B \rightarrow 1886$

$B \rightarrow 988 \text{ more than } A$

*Qn: A?*

Think (What is my plan?)

✓ Can I use Model Drawing?

Can I look for a pattern?

Can I work backwards?

Can I use Guess and Check?

Other heuristic(s) I can use:

---

# Q4: Model Drawing

## (Comparison with 2 variables – Unequal Distribution)

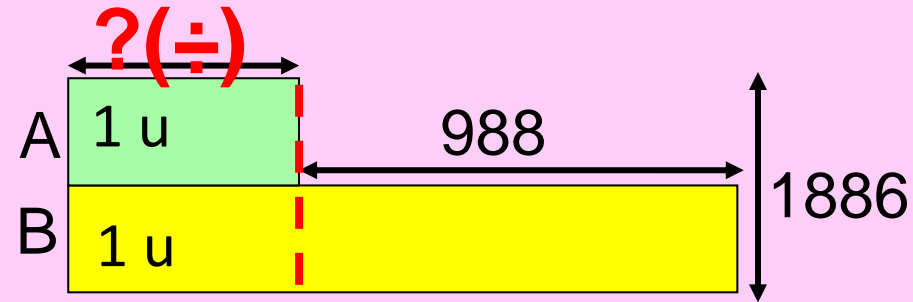
See (What is given?)

$A + B \rightarrow 1886$

$B \rightarrow 988$  more than  $A$

Qn:  $A$ ?

Act (What do I need to do?)



$$1886 - 988 = 898$$

$$2 u = 898$$

$$1 u = 898 \div 2$$

$$= 449$$

Worker A sorted **449** bottles in the morning.



# Q4: Model Drawing

## (Comparison with 2 variables – Unequal Distribution)

At a factory, Worker A and Worker B sorted 1886 plastic bottles altogether. Worker B sorted 988 more bottles than Worker A. How many bottles did Worker A sort?

### Act

$$1886 - 988 = 898$$

$$2 \text{ u} = 898$$

$$1 \text{ u} = 898 \div 2 \\ = 449$$

### Relook (Reflect and Check)

$$1 \text{ u} = 449$$

$$2 \text{ u} = 449 \times 2 = 898$$

$$898 + 988 = 1886 \checkmark \text{ok}$$

Worker A sorted 449 bottles in the morning.

C	✓
O	✓
U	✓
R	✓
T	✓

## Q5: Unitary Method (Find Total)

Alex ran 234 m. Roy jogged thrice the distance ran by Alex. What was the total distance run by both Alex and Roy?

**See (What is given?)**

Alex → 234 m

Roy → 3x the distance ran  
by Alex

Qn: Total distance ran?

**Think (What is my plan?)**

- ✓ Can I use Model Drawing?
  - Can I look for a pattern?
  - Can I work backwards?
  - Can I use Guess and Check?
  - Other heuristic(s) I can use:
-

## Q5: Unitary Method (Find Total)

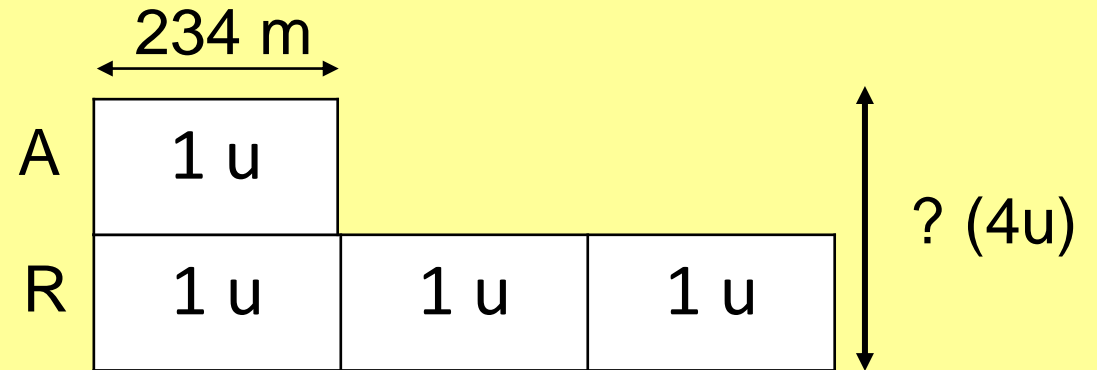
See (What is given?)

Alex  $\rightarrow$  234 m

Roy  $\rightarrow$  3x the distance ran  
by Alex

Qn: Total distance ran?

Act (What do I need to do?)



Method 1

$$1 \text{ u} = 234 \text{ m}$$

$$3 \text{ u} = 3 \times 234 \text{ m} \\ = 702 \text{ m}$$

$$234 \text{ m} + 702 \text{ m} = 936 \text{ m}$$

Method 2

$$1 \text{ u} = 234 \text{ m}$$

$$4 \text{ u} = 4 \times 234 \text{ m} \\ = 936 \text{ m}$$

They ran **936 m** altogether.



## Q5: Unitary Method (Find Total)

Alex ran 234 m. Roy jogged thrice the distance ran by Alex. What is the total distance ran by both Alex and Roy?

Act

Method 2

$$1 \text{ u} = 234 \text{ m}$$

$$\begin{aligned} 4 \text{ u} &= 4 \times 234 \text{ m} \\ &= 936 \text{ m} \end{aligned}$$

Relook (Reflect and Check)

$$4 \text{ u} = 936$$

$$\begin{aligned} \text{Alex} \rightarrow 1 \text{ u} &= 936 \div 4 \\ &= 234 \checkmark \text{ok} \end{aligned}$$

They ran **936 m** altogether.

C	✓
O	✓
U	✓
R	✓
T	✓

## Q6: Unitary Method

A bookshop sold 212 pencils and pens in a day. The number of pens sold was thrice the number of pencils sold. How many pencils were sold ?

See (What is given?)

Pencils and Pens  $\rightarrow$  212

Pens  $\rightarrow$  3x as many as Pencils

Qn: ? Pencils were sold

Think (What is my plan?)

✓ Can I use Model Drawing?

Can I look for a pattern?

Can I work backwards?

Can I use Guess and Check?

Other heuristic(s) I can use:

---

# Q6: Unitary Method

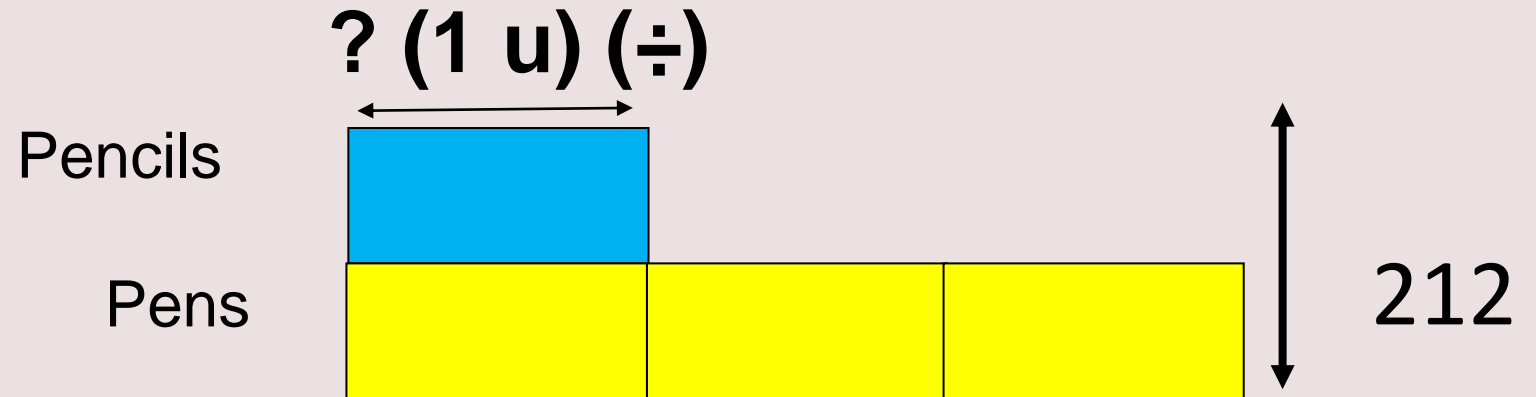
Act (What do I need to do?)

See (What is given?)

pencils and pens → 212

pens → 3x as many as pencils

Qn: ? Pencils were sold



Method

$$4 \text{ u} = 212$$

$$1 \text{ u} = 212 \div 4$$

$$= 53$$

**53** pencils were sold.



## Q6: Unitary Method

A bookshop sold 212 pencils and pens in a day. The number of pens sold was thrice the number of pencils sold. How many pencils were sold ?

Act

Method

$$4 \text{ u} = 212$$

$$\begin{aligned} 1 \text{ u} &= 212 \div 4 \\ &= 53 \end{aligned}$$

Relook (Reflect and Check)

$$1 \text{ u} = 53$$

$$\begin{aligned} 4 \text{ u} &= 4 \times 53 \\ &= 212 \checkmark \text{ok} \end{aligned}$$

C	<input checked="" type="checkbox"/>
O	<input checked="" type="checkbox"/>
U	<input checked="" type="checkbox"/>
R	<input checked="" type="checkbox"/>
T	<input checked="" type="checkbox"/>

53 pencils were sold.

## Q7: Model Drawing (Stacking Model)

A pair of shoes and 3 bags cost \$60. The pair of shoes cost twice as much as the bag. Find the cost of the pair of shoes.

See (What is given?)

$$1S + 3B \rightarrow \$60$$

$$1S \rightarrow 1B \times 2$$

*Qn: 1S ?*

Think (What is my plan?)

Can I use Part-Whole Model Drawing?

Can I use Comparison Model Drawing?

Can I use Stacking method? ✓

Can I act it out?

Can I use Guess and Check?

Can I use Working Backwards?

Other heuristic(s) I can use:

# Q7: Model Drawing (Stacking Model)

A pair of shoes and 3 bags cost \$60. The pair of shoes cost twice as much as the bag. Find the cost of the pair of shoes.

Act (What do I need to do?)

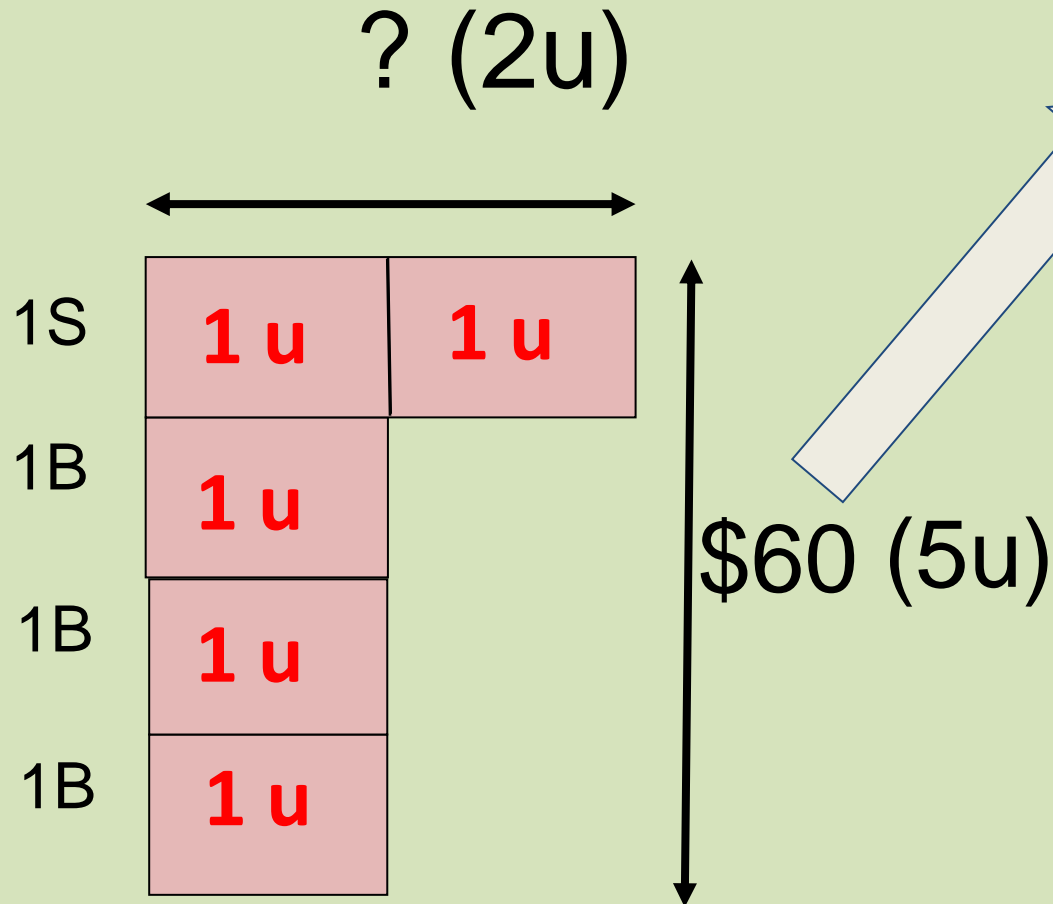
**MATCH**

$$5u = \$60$$

$$1u = \$60 \div 5 = \$12 \text{ (BAG)}$$

$$2u = \$12 \times 2 = \underline{\underline{\$24 \text{ (SHOE)}}}$$

The pair of shoes cost \$24.



# Q7: Model Drawing (Stacking Model)

## Relook (Reflect and Check)

$$\$24 + \$12 + \$12 + \$12 = \$60$$

✓ok

C	✓
O	✓
U	✓
R	✓
T	✓



## Q8: Model Drawing (Stacking Model)

Mr Koh paid \$1145 for a dining table and 4 chairs.

The table cost \$270 more than each chair.

What was the cost of each chair?

See (What is given?)

$$1T + 4C \rightarrow \$1145$$

$$1T \rightarrow 1C + \$270$$

*Qn: 1C ?*

Think (What is my plan?)

Can I use Part-Whole Model Drawing?

Can I use Comparison Model Drawing?

Can I use Stacking method? ✓

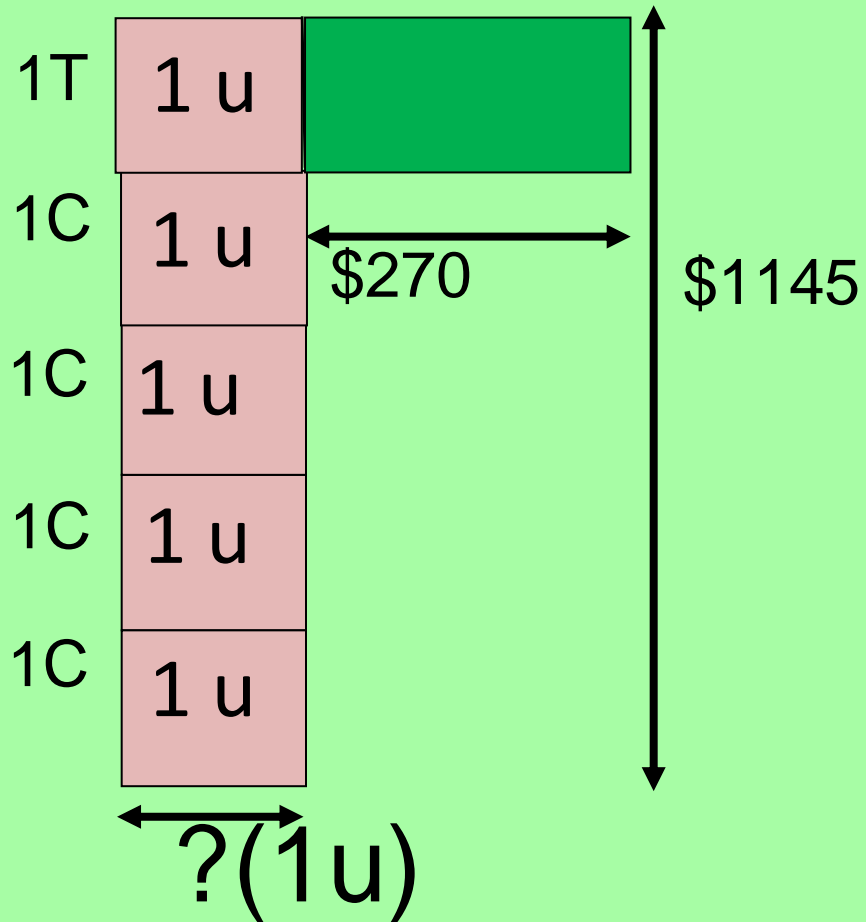
Can I act it out?

Can I use Guess and Check?

Can I use Working Backwards?

Other heuristic(s) I can use:

## Q8: Model Drawing (Stacking Model)



Act (What do I need to do?)

$$\$1145 - \$270 = \$875$$

MATCH

$$5u = \$875$$

$$1u = \$875 \div 5 = \$175$$

A chair cost **\$175.**

# Q8: Model Drawing (Stacking Model)

Relook (Reflect and Check)

$$\begin{aligned}\text{Table} &\rightarrow \$175 + \$270 \\ &= \$445\end{aligned}$$

$$\begin{aligned}4 \text{ chairs} &\rightarrow 4 \times \$175 \\ &= \$700\end{aligned}$$

$$\begin{aligned}\text{Total cost} &\rightarrow \$445 + \$700 \\ &= \$1145 \checkmark \text{ok}\end{aligned}$$

C	✓
O	✓
U	✓
R	✓
T	✓

## Q9: Model Drawing (Fraction of a Set)

Annie baked 252 cookies.  $\frac{4}{7}$  of the cookies were chocolate cookies and the rest were butter cookies. How many butter cookies did she bake?

See (What is given?)

Total → 252 cookies

Chocolate →  $\frac{4}{7}$  of the cookies

Rest → Butter cookies

*Qn: Number of butter cookies?*

Think (What is my plan?)

Model drawing ✓

Working backwards

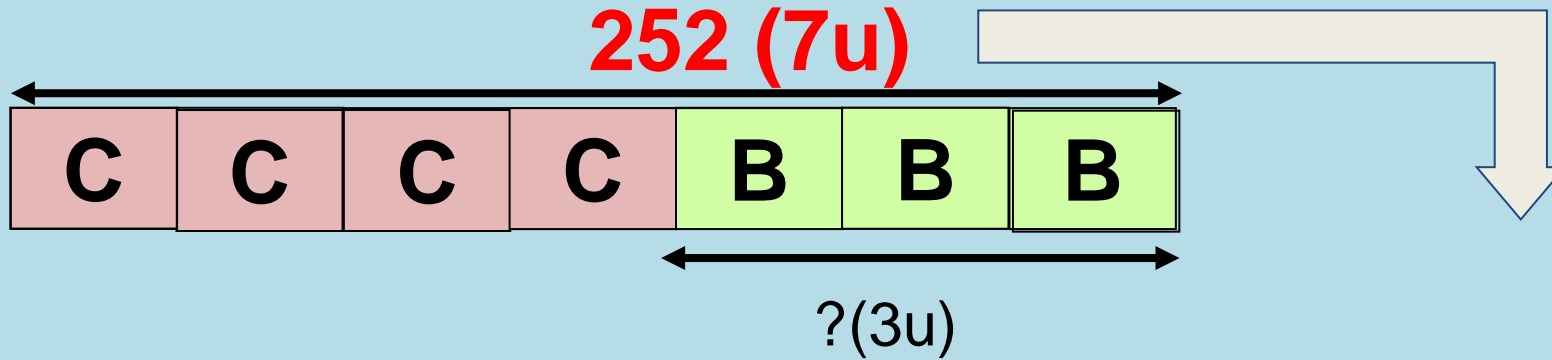
Restate the problem

Stacking Method



## Q9: Model Drawing (Fraction of a Set)

Act (What do I need to do?)



**MATCH**

$$7u = 252$$

$$1u = 252 \div 7 = 36$$

$$3u = 36 \times 3 = \underline{108}$$

She baked 108 butter cookies.

## Q9: Model Drawing (Fraction of a Set)

### Relook (Reflect and Check)

$$108 \div 3 = 36$$

$$36 \times 7 = 252$$

✓ok

C	✓
O	✓
U	✓
R	✓
T	✓

## Q10: Model Drawing (Fraction of a Set)

Mrs Liz had a birthday party.  $\frac{3}{5}$  of the children were girls. There were 36 boys at the party. How many children were there altogether?

See (What is given?)

Girls  $\rightarrow \frac{3}{5}$  of the children

Boys  $\rightarrow 36$

*Qn: total number of children ?*

Think (What is my plan?)

Model drawing ✓

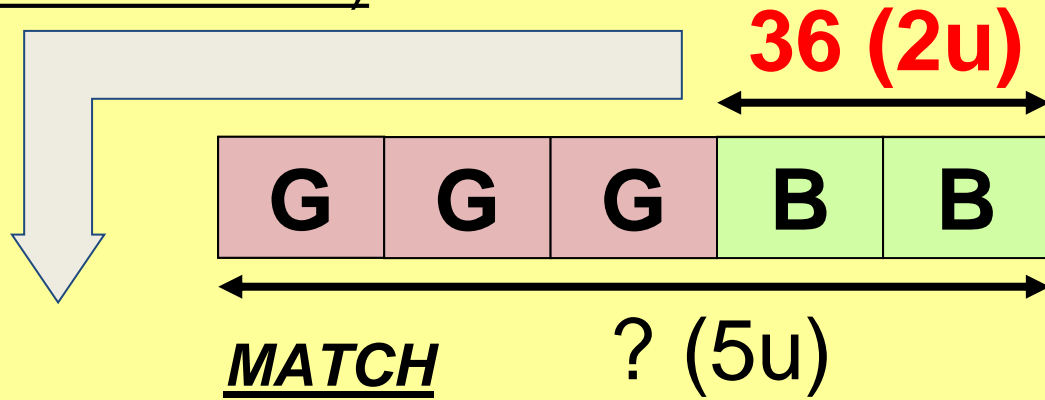
Working backwards

Restate the problem

Stacking Method

# Q10: Model Drawing (Fraction of a Set)

Act (What do I need to do?)



$$2 u = 36$$

$$1 u = 36 \div 2 = 18$$

$$5 u = 18 \times 5 = \underline{90}$$

There were 90 children altogether.

# Q10: Model Drawing (Fraction of a Set)

## Relook (Reflect and Check)

$$90 \div 5 = 18$$

$$18 \times 2 = 36$$

✓ok

C	✓
O	✓
U	✓
R	✓
T	✓



## Q11: Model Drawing (Fraction of a Set)

There are men and women in a room,  $\frac{7}{8}$  of the people were men.

There were 72 more men than women. How many people were there in the room altogether?

See (What is given?)

$M \rightarrow \frac{7}{8}$  of the people

$$M - W = 72$$

Think (What is my plan?)

Model drawing ✓

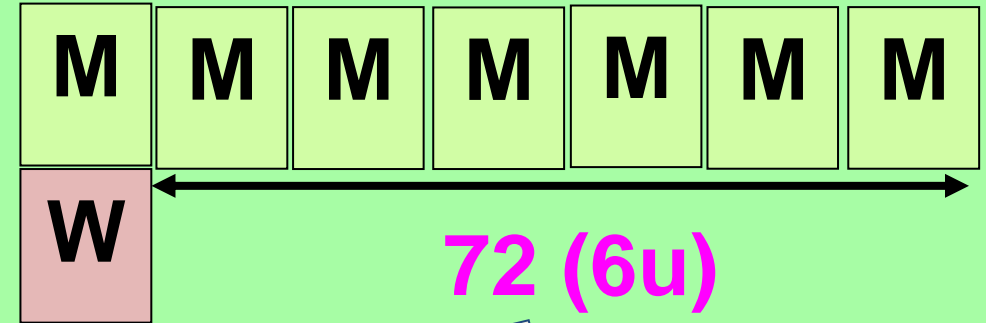
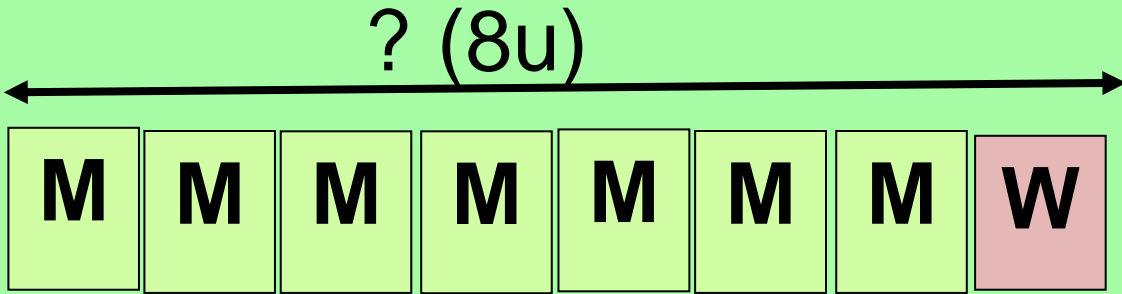
Working backwards

Restate the problem

Stacking Method

*Qn: total number of children ?*

# Q11: Model Drawing (Fraction of a Set)



Act (What do I need to do?)

$$6u = 72$$

$$1u = 72 \div 6 = 12$$

$$8u = 12 \times 8 = \underline{96}$$

There were 96 people altogether.

# Q11: Model Drawing (Fraction of a Set)

Relook (Reflect and Check)

$$M \rightarrow 7 \times 12 = 84$$

$$W \rightarrow 12$$

$$M - W = 84 - 12 = 72 \quad \checkmark \text{ok}$$

C	✓
O	✓
U	✓
R	✓
T	✓

# Q12: Model Drawing (Before and After) – Make Equal

Samy has 250 erasers and Darryl has 64 erasers. How many erasers must Samy give to Darryl so that both have the same number of erasers?

See (What is given?)

S  $\rightarrow$  250

D  $\rightarrow$  64

S give ? to D so that  $S = D$

Think (What is my plan?)

- ✓ Can I use Model Drawing?
  - Can I look for a pattern?
  - Can I work backwards?
  - Can I use Guess and Check?
  - Other heuristic(s) I can use:
-

# Q12: Model Drawing (Before and After) – Make Equal

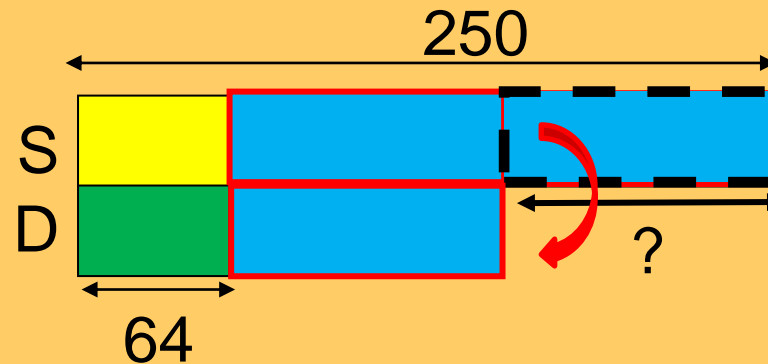
See (What is given?)

S  $\rightarrow$  250

D  $\rightarrow$  64

S give ? to D so that  
 $S = D$

Act (What do I need to do?)



$$250 - 64 = 186$$

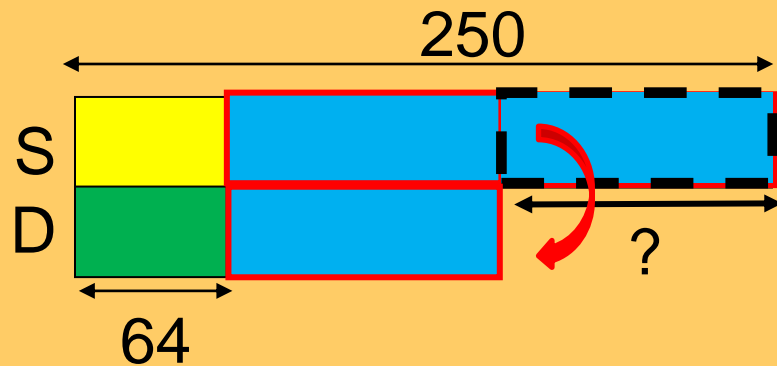
$$186 \div 2 = \mathbf{93}$$

Samy must give Darryl 93 erasers.



# Q12: Model Drawing (Before and After) – Make Equal

Samy has 250 erasers and Darryl has 64 erasers. How many erasers must Samy give to Darryl so that both have the same number of erasers?



Act

$$250 - 64 = 186$$

$$186 \div 2 = 93$$

Relook (Reflect and Check)

$$250 - 93 = 157$$

$$64 + 93 = 157 \checkmark \text{ok}$$

Samy must give Darryl 93 erasers.

C	✓
O	✓
U	✓
R	✓
T	✓

# Q13: Model Drawing (Before and After) – Before Equal

Ariel had as many roses as Belle.

After Ariel gave 64 roses away, Belle had 5 times as many roses as Ariel.

How many roses did Ariel have at first?

**See (What is given?)**

Before :  $A = B$

After A gave 64,  $B \rightarrow 5 \times A$

Before : A ?

**Think (What is my plan?)**

✓ Can I use Model Drawing?

Can I look for a pattern?

Can I work backwards?

Can I use Guess and Check?

Other heuristic(s) I can use:

---

# Q13: Model Drawing (Before and After) – Before Equal

See (What is given?)

Before :  $A = B$

After A gave 64,  $B \rightarrow 5 \times A$

Before : A ?

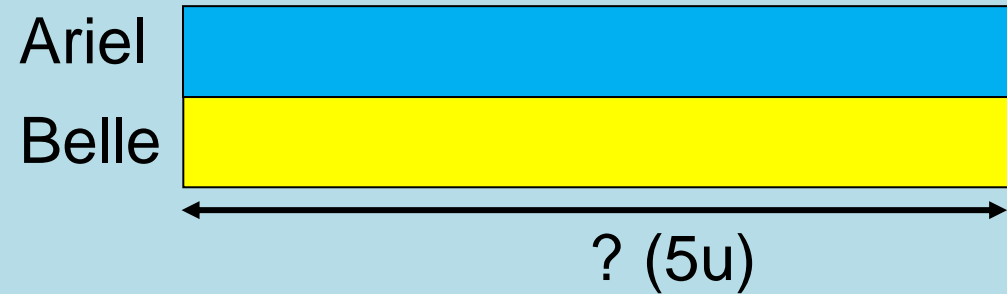
$$4u = 64$$

$$1u = 64 \div 4 = 16$$

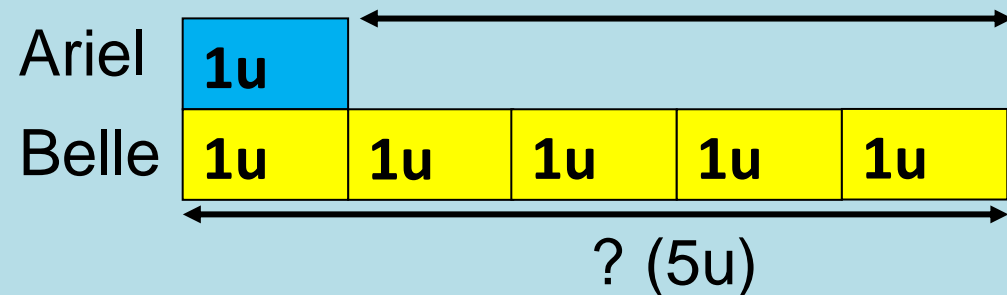
$$5u = 5 \times 16 = 80$$

Act (What do I need to do?)

Before



After



Ariel had **80** roses at first.

# Q13 : Model Drawing (Before and After) – Before Equal

Ariel had as many roses as Belle.

After Ariel gave 64 roses away, Belle had 5 times as many roses as Ariel.

How many roses did Ariel have at first?

## Act

$$4 \text{ u} = 64$$

$$1 \text{ u} = 64 \div 4 = 16$$

$$5 \text{ u} = 5 \times 16 = 80$$

## Relook (Reflect and Check)

$$1 \text{ u} = 80 \div 5 = 16$$

$$4 \text{ u} = 16 \times 4 = 64 \quad \checkmark \text{ok}$$

Ariel had **80** roses at first.

C	✓
O	✓
U	✓
R	✓
T	✓

# Welcome to KooBits







Joewen Teo

Junyuan Primary School

0 XP  
Lvl 1



Brain Games



Events



Story

**Daily Challenge**  
10 personalized questions per day

Start

Mission

Multiplayer

Assignment



0  
Total CPs



1000  
KoKo Credits



Daily Bonus



Switch to Teacher



